Tensile Deformation and Failure Behavior of Open Cell Nickel and Copper Foams

Shojiro Ochiai¹, Satoshi Nakano¹,* Yuya Fukazawa¹,*, Mohamed Shehata Aly¹, Hiroshi Okuda¹, Komei Kato², Takeshi Isobe³, Koichi Kita⁴ and Keiichi Honma³

¹Department of Materials Science and Engineering, Kyoto University, Kyoto 606-8501, Japan
²Mitsubishi Materials Corporation, Saitama 330-8508, Japan
³Non-Ferrous Alloys Research & Technology Laboratory, Mitsubishi Materials Corporation, Kitamoto 364-0023, Japan
⁴Central Research Institute, Mitsubishi Materials Corporation, Kitamoto 364-0022, Japan

Keywords: nickel foam, copper foam, deformation and failure process

(Received November 19, 2009; Accepted January 19, 2010; Published March 3, 2010)

Tensile deformation and failure behavior at room temperature of the open cell nickel and copper foams with high porosity (~96%) fabricated with the slurry foaming process at Mitsubishi Materials Corporation, Japan, was studied. In-situ observation of the deformation and failure behavior was conducted with a digital microscope. Stress-strain curves were measured, in which a non-contact extensometer was employed to detect the strain of the samples accurately. Electric resistance was measured to monitor the damage evolution. Finite element stress analysis was conducted to calculate the morphological change of cells with applied strain and the stress distribution in cells. It was revealed that the deformation and failure progressed through the following four stages; stage I characterized by the elastic deformation, stage II by plastic deformation, stage III by the occurrence of plastic deformation and cumulative failure of struts and stage IV by the chain reaction of strut failure nearly in a limited cross-section, respectively. Also it was found that the distribution of failure strain of struts in stage III, measured from the serrations in the stress-strain curve, could be described by the Weibull distribution, with which the transition from stage II to III was identified. Also, the result of the statistical analysis suggested that the average failure strain of the struts in the foam is much higher than the strain at ultimate stress of the foam.

1. Introduction

As the metal foams have the specific features such as light weight, high specific surface area, high potential to absorb impact energy, high air and water permeability and good acoustic insulating properties and so on, they are attractive for industrial application to light weight construction, crash energy absorption, noise control, and also during service, due to which the mechanical behavior is one of the most important research subjects.

Until now, a wide variety of manufacturing methods, such as gas-injection method⁴,⁵ directional solidification method⁶,⁷ precursor method⁸⁹, slurry foaming method¹⁰ and so on¹²¹⁵ has been developed. Among them, the slurry foaming method, in which the metal powders with specific particle size are admixed at room temperature with a foaming agent to form foamy slurry, and the green samples are dried and then sintered under controlled atmosphere at high temperature. This method produces open cell structure with very high porosity fraction (90~97%).¹¹ In the present work, the nickel and copper foams manufactured by this method were studied to reveal the deformation and failure process.

2. Experimental and Analytical Procedure

Open cell nickel and copper foam-plates with porosity volume fraction ~96% and average pore size ~600 μm, fabricated by the slurry foaming method¹¹ at Mitsubishi Materials Corporation, were used. The thicknesses of the nickel and copper foam plates were 2.0 and 1.5 mm on average, respectively. The structure of the (a) nickel and (b) copper foams is shown in Fig. 1. The cell structure is composed of struts and nodes as indicated in Fig. 1(a).

Tensile test was carried out at room temperature with a tensile machine (AUTOGRAPH-AG 50kNG, Shimadzu Corp). The width and whole length of tensile samples were 10 and 120 mm, respectively. Both ends of the tensile samples are glued to aluminum tabs with an epoxy-glue, as shown in Fig. 2(a). The test was conducted at a constant crosshead speed of 8.3 × 10⁻⁵ m·s⁻¹.

Strain of samples was measured with a non-contact extensometer due to the following reasons. The porosity volume fraction of the present samples was high (~96%) and the metals (pure nickel and copper) were soft. The strain gages were not suitable for measurement of the sample strain due to the constraint, even small, of the deformation of cells at the gage-adhered parts and due to the narrow covered area which gives, more or less, only local information. The usual extensometer was also not suitable due to its weight that can cause bending of samples. In the measurement of the strain of the sample itself with a non-contact extensometer, two markers made of paper were pasted on the samples, whose spacing was 50 mm, as shown in Fig. 2(a). The displacement of the markers was recorded with a laser CCD camera (DVW-200 Shimadzu), as shown in Fig. 2(b).

To monitor the progress of failure, the change of the electric resistance with strain was measured with a usual four probe method. The deformation and failure behavior was observed in-situ with a digital microscope (KEYENCE VHX-500SP1639).

The changes of the morphology of the cell and stress distribution in the deformed cell were analyzed with a finite
element analysis. Figure 3(a) and (b) shows the observed shapes of the non-damaged and damaged cells in the copper foam, respectively. The observed morphologies were modeled as shown in the right sides to calculate the stress state. Hereafter the model in (a) is called as the cell model without a failed strut and that in (b) as the cell model with a failed strut. In this modeling, two dimensional model was used in accordance with the two dimensional observation. Though the present modeling is rough, the experimentally observed morphological change of cells could be reproduced and also important indications concerning the stress-state could be read, as will be shown later in 3.3. As the externally applied strain is transferred to the cell mainly by the struts parallel to the tensile axis, the boundary conditions were given as shown in the models in Fig. 3. The stress analysis was carried out using a commercial finite element code MARC/Mentat under the plane stress condition. The yielding condition for the copper was given by the von Mises criterion.

As the mechanical properties of the copper in the present foam were unknown, the following values reported for full annealed polycrystalline copper[16] were used: Young’s modulus $E_{\text{Cu}} = 110$ GPa, Poisson’s ratio $\nu = 0.343$, tensile strength ($\sigma_{\text{UTS}}$) = 210 MPa, yield stress ($\sigma_Y$) = 33.3 MPa and nominal strain at ultimate stress ($\epsilon_{\text{UTS}}$) = 60%. From these reported values, the true stress ($\sigma$)-true strain ($\epsilon$) curve of copper was expressed with the Ludwik’s equation given by

$$\sigma = \sigma_Y + K(\epsilon - \epsilon_Y)^n$$  \hspace{1cm} (1)

where $\epsilon_Y$ is the yield strain, and $K$ and $n$ are the constants. Using the well known expressions in solid mechanics, we have $\epsilon_Y = \sigma_Y/E_{\text{Cu}}$ (Hooke’s law), $\epsilon = \ln(1 + \epsilon)$ (relation...
between the true ($\varepsilon$) and nominal ($\varepsilon$) strains, $\sigma_{UTS} = \left(\sigma_f + K(\varepsilon_{UTS} - \varepsilon_f)^n\right) \exp(-\varepsilon_{UTS})$ (relation of the nominal tensile strength ($\sigma_{UTS}$) to the true strain ($\varepsilon_{UTS}$) at ultimate stress), and $[d(\sigma_f \exp(-\varepsilon)/d\varepsilon)]/d\varepsilon = 0$ at $\varepsilon = \varepsilon_{UTS}$ (necking condition). Substituting the reported mechanical property values mentioned above into these relations, we had $\varepsilon_f = 3.03 \times 10^{-4}$ ($\sigma_f = 33.3$ MPa), $n = 0.467$ and $K = 432$ MPa for eq. (1).

3. Results and Discussion

3.1 Stress-strain curve and change of electric resistance with strain

The nominal stress-nominal strain and electric resistance-nominal strain curves, measured at the same time, of the nickel- and copper-foams are presented in Fig. 4(a) and (b), respectively. The stress-strain curve in the rectangle in Fig. 4(b) is presented at high magnification in Fig. 4(c). The following features are found in Fig. 4.

(1) In the initial stage, the foams deform elastically. The strain range of this stage was very narrow, around 0.01% for both foams.

(2) After yielding, the most parts of foams deform plastically, as shown later in 3.3. With further increasing applied strain, serrations appear in the stress-strain curve as shown in (c), in which the serrated parts are shown with circles. Such serrations are attributed to the failure mainly of the struts, as ascertained by the observation (details will be presented later in 3.2). In each serration, the stress drops due to the strut failure-induced loss of stress carrying capacity of the foams and then increases due to the strain hardening of the constituting metals. In the strain range up to the strain at ultimate stress (5.2 and 6.2% for nickel and copper foams, respectively), the stress increases after each serration. This means that the failure of struts occurs independently to each other and is cumulated in the sample up to the strain at ultimate stress. In other words, even when the struts are failed, they do not cause successive failure of the neighboring struts. Such a failure mode is named as cumulative mode. On the other hand, beyond the strain at ultimate stress, the stress of the foams decreases with increasing strain, suggesting that the failure of struts occurs in the manner to reduce the stress carrying capacity of the foams. As will be shown in 3.2, the failure of the struts occurs successively in a limited cross-section beyond the strain at ultimate stress (successive failure mode). Namely, the failure mode of the struts turns at the strain at ultimate stress from cumulative to successive one.

(3) The electric resistance increases gradually up to the strain at ultimate stress. On the other hand, beyond the strain at ultimate stress, the resistance increases significantly, reflecting the successive failure of struts in a limited cross-section. This means that, when the failure of the struts occurs in a limited cross-section, the current path decreases significantly. The gradual increase in resistance below the strain at ultimate stress is attributed to the failure of the struts and also to the increase in amount of dislocations. The individual effect could not be estimated separately in the present work. However, judging from the significant increase in resistance beyond the strain at ultimate stress, stemming from the failure of the struts in a limited cross-section, it is speculated that the gradual increase in resistance below the strain at ultimate stress stems mainly from the spatially distributed failure of the struts in the specimen volume.

(4) The features mentioned above suggest that the deformation and failure progresses through the following four stages; stage I characterized by the elastic deformation, stage II by plastic deformation without failure of struts, stage III by the co-occurrence of plastic deformation and cell failure and stage IV by the successive failure of struts nearly in a limited cross-section, as marked in Fig. 4(a) and (b) for nickel and copper foams, respectively.

Details of the in-situ observation results on the failure behavior in the late stage III and stage IV will be presented in 3.2. The change of the shape of cells with increasing applied strain and the stress distribution calculated with a finite element analysis for the model cells in Fig. 3 will be presented in 3.3. An attempt to estimate the strain at transition from stage II to III, based on the statistical
analysis, will be presented in 3.4. Also the condition for the 
transition of stage III to IV to arise will be discussed in 3.4.

3.2 Observed deformation and failure behavior

Figure 5 shows the morphological change of the foam with 
increasing applied strain. The shape of the cells is complex, 
due to which complex stress state is realized, as has been 
observed by X-ray tomography for other type aluminum 
foams.17,18) From the phenomenological viewpoint, the cells 
are evidently elongated and the struts are straight forwarded 
along the tensile direction. As shown in Fig. 4, the strain 
range of elastic deformation (stage I up to around 0.01% 
strain in both nickel and copper foams) is very narrow. The 
morphological change is eternal once applied strain exceeds 
around 0.01%.

The ductile nature of the struts was evidenced by the 
failure morphology. Both the nickel and copper foams failed 
similarly in a ductile manner. Figure 6 shows (a) the overall 
failure surface and (b), (c) failure morphology of the struts in 
the nickel foam. As shown in (a), the overall failure occurred 
nearly in a limited cross-section where the difference in 
height of the failed struts was within one cell size. The reason 
for this will be discussed in detail later in this sub-section. 
The struts failed in a ductile manner, accompanied by (b) the 
cup and cone type and (c) shear lip type morphology. The 
struts in the present foam are composed of a small number of 
grains in a cross-section. It is deduced that the crystallo-
graphic relation between the grain and tensile direction in (b) 
is different from that in (c), causing the different failure 
morphology. In (b), plural slip systems are found and the slip 
bands are wavy. In this case, possibly due to the intersection 
of dislocations, voids are formed, resulting in cup and cone 
type ductile failure. On the other hand, in (c), only one slip 
band failure occurs. In this case, a shear lip failure occurs.

Figure 7 shows the in-situ observation result of the failure 
process of the nickel foam in stage IV where the struts are 
failed successively in a limited cross-section. (a) to (e) were 
observed at the applied strains $e = 5.0, 5.3, 5.6, 6.0$ and 
6.6%, respectively. The transition of the failure mode of 
struts from cumulative to successive occurred at $e = 5.2%$. 
In this specimen, the strut having a portion with a very 
narrow cross-section, indicated by 1 in (a), is failed as 
shown in (b). Once the strut 1 is failed, the failed-ends in the 
strut 1 open and the strut 2 originally nearly perpendicular 
to the tensile direction (b) is elongated toward the direction 
parallel to the tensile stress (c). As a result, the strut 3 in (c) 
is stressed more and is failed (d). In this way, the failure of 
one strut (1 in this specimen) causes the failure of the 
neighboring strut 3. After the failure of the strut 3, the 
failed-ends open, which gives high stress to the strut 4. As a 
result, the strut 4 is failed. Due to such a chain reaction, the 
neighboring struts are failed successively one after another 
nearly in a limited cross-section within one cell size in the 
stress direction. The reason for this is accounted for as 
follows.

As the cross-sectional area of surviving struts varies along 
the sample length direction and the stress concentration of 
the surviving struts enhanced by the preceding failure of the 
neighboring struts also varies along the length direction, the 
failure position of each strut is different, namely failure of the 
foam progresses in a zigzag manner, but as the latter (stress 
concentration) is enhanced essentially in the struts between 
upper and lower nodes, the difference in height among the 
failed struts is within one cell size. Thus, the successive 
failure of struts in stage IV occurs nearly in a limited cross-
section. The failure of the copper foam in stage IV occurs in a 
same manner to that of the nickel foam (failure of one strut 
causes the neighboring struts one after another nearly in a 
limited cross-section.).
In this way, the morphology change of cells and failure of struts take place in the deformation and failure process of ductile metal foams. The deformation and failure process both of the nickel and copper foams observed in the present work is summarized, as schematically shown in Fig. 8.

3.3 Change of the morphology and stress distribution with increasing applied strain in the cell with and without a failed strut, analyzed with the finite element method

The results analyzed with the finite element analysis using the models of the cell without and with a failed strut shown in Fig. 3(a) and (b) are presented in Figs. 9 and 10, respectively. In these figures, the true stress in the tensile direction is used representatively instead of the equivalent stress, since the tensile and compressive stresses co-exist, which cannot be distinguished if we use the equivalent stress. Initial shape of the cell is also indicated with black lines for comparison. The following features are read from Figs. 9 and 10.

1. Both cells without and with a failed strut are elongated more in the tensile direction with increasing applied strain. These results are in good accordance with the observation results in Figs. 5 and 7.
2. In the cell without a failed strut (Fig. 9), tensile stress is exerted in the inner side parts and compressive one in the outer side parts in both struts, as shown in (A) and (B) indicated with blue broken lines in (a). This means that bending stress acts in both struts during elongation of the cell in the tensile direction, stemming from the curved shape of the struts in the original state. With further increasing applied...
strain, the struts elongate along the tensile direction and the compressive stress tends to be diminished.

(3) In the cell with a failed strut (Fig. 10), the opening of the failure ends in the strut increases with increasing applied strain. This phenomenon is in good accordance with the observation result in Fig. 7. It is noted that such an opening enhances the tensile stress of the surviving (non-failed) strut as shown in the green circles in Fig. 10(c) and (d). This result accounts well for the successive failure of struts in stage IV observed in Fig. 7.

3.4 Statistical analysis of failure strain of struts

It has been shown in 3.1 and 3.2 that the failure of the struts occurs cumulatively and successively below and beyond the strain at ultimate stress, respectively. Also it has been shown in 3.3, when a strut fails, the failure ends open, raising the stress concentration at the neighboring struts with increasing applied strain. As shown in these results, the failure of struts plays a dominant role in the determination of failure process and mechanical properties of foams. However, the statistical feature of failure of struts has not been studied in detail until now. In this sub-section, the failure strain of struts in the foam is analyzed statistically. Then, the result is used to determine the initiation of the strut failure, namely the transition strain from stage II to stage III (Figs. 4(a) and (b)) and also to account for the transition from stage III to IV.

As has been shown in Fig. 4(c), the cumulative failure of the struts in stage III is reflected with the serrations in the stress-strain curve. Thus the failure strain $\varepsilon_f$ of the strut in the foam can be read from the serration. The $\varepsilon_f$ value in this work...
is not the usual failure strain for straight samples. It is dependent on the geometrical relation of the strut to the applied tensile stress direction. For instance, when the strut is just parallel to the tensile axis, the externally applied stress is transferred efficiently and it can be failed at its failure strain. On the other hand, when the strut is largely inclined to the tensile axis, the applied stress is consumed until the stress is transferred efficiently, as in the case of loose strands. Namely the strut needs high strain to be stretched tightly. In the present work, such a geometry-affected failure strain $e_f$ is estimated from the serration.

In the present samples, the stress-strain curves were measured for the test pieces shown in Fig. 2(a). The serrations in the stress-strain curve (Fig. 4(c)) arose from the volume of $10$ (width) $\times 50$ (length) $\times 2.0$ (thickness) mm$^3$ for the nickel foam and from the volume of $10 \times 50 \times 1.5$ mm$^3$ for the copper foam. The average pore size was 600$\mu$m for both foams. Thus, as a first approximation, total number $n$ of struts in the gage portion, for which the stress-strain curve was measured, was taken to be $n = 4648$ and 3486 for nickel and copper foams, respectively. The cumulative probability $F_i$ of $e_f$ of the $i^{th}$-failed strut was estimated by the median rank method, expressed by

$$F_i = (i - 0.3)/(n + 0.4) \quad (2)$$

For description of distribution of the $e_f$ values, three parameter Weibull distribution function,\(^{19}\) which has been used widely for description of strength distribution of materials, was used as a first approximation in this work. According to this function, the cumulative probability $F$ of $e_f$ is expressed by

$$F = 1 - \exp[-{(e_f - e_{f,\text{min}})/e_0}^m] \quad (3)$$

where $e_0$ and $m$ are the scale and shape parameters, respectively, and $e_{f,\text{min}}$ is the lower bound of $e_f$. The parameter values of $e_0$, $m$ and $e_{f,\text{min}}$ were estimated as follows.

Equation (3) is re-written in the form,

$$\ln (1 - F)^{-1} = m \ln (e_f - e_{f,\text{min}}) - m \ln (e_0). \quad (4)$$

First, various values were assumed for $e_{f,\text{min}}$ and the linearity between $\ln (1 - F)^{-1}$ and $\ln (e_f - e_{f,\text{min}})$ was examined for each $e_{f,\text{min}}$-value. The $e_{f,\text{min}}$-value that gave the highest linearity was estimated as the $e_{f,\text{min}}$. We had $e_{f,\text{min}} = 1.7\%$ for nickel foam and $0.86\%$ for copper foam. For these values, very high linearity is found in the relation of $\ln (1 - F)^{-1}$ to $\ln (e_f - e_{f,\text{min}})$, as shown in Fig. 11. The $m$ and $e_0$ were estimated from the slope and extrapolation of the relation of $\ln (1 - F)^{-1}$ to $\ln (e_f - e_{f,\text{min}})$, as indicated in Fig. 11.

As shown above, the values of $e_{f,\text{min}}$, $m$ and $e_0$ were obtained for the assumed number of struts ($n = 4648$ (nickel) and $n = 3486$ (copper) were calculated using the average cell size). The calculated $n$ corresponds to the minimum case for $n$ among the possible cases since each cell has plural struts. The actual $n$ value is larger. The influence of the $n$ value on the Weibull plot was examined as follows.

Figure 12 shows the Weibull plot in the nickel foam for $n = 4648$, 13944 (three times of 4648) and 46480 (ten times), obtained by the procedure stated above. The $e_{f,\text{min}}$ and $m$ values were not affected by $n$. On the other hand, $e_0$ value was dependent on $n$: the larger the $n$, the larger became the $e_0$. This result indicates that the obtained value $e_{f,\text{min}} = 0.017$...
and \( m = 2.9 \) are reliable even when the actual \( n \) value is unknown, while \( e_0 \) value is dependent on \( n \) value and it shall be determined for an actual \( n \) value.

The reason for this is accounted for as follows. In stage III, the struts with low failure strains are failed cumulatively. In this stage, the number of failed struts is small in comparison with the total number of struts. Thus, eq. (3) is reduced to

\[
F = \left( e_t - e_{t,\text{min}} / e_0 \right)^m
\]

Also, as \( F \) is low, the term \( \ln \ln(1 - F)^{-1} \) in eq. (4) is reduced to \( \ln(F) \). The reduced form of eq. (4) is just same as eq. (5).

As the measured \( e_t \) values are common for any \( n \) value (and for \( F \) since \( F \) is given by eq. (2)), the \( e_{t,\text{min}} \) value that gives highest linearity between \( \ln \ln(1 - F)^{-1} \) (= \( \ln(F) \) in the reduced form) and \( \ln(e_t - e_{t,\text{min}}) \) in eq. (4) is estimated uniquely regardless the range of \( F \) concerned. Once \( e_{t,\text{min}} \) value is obtained, the slope of the \( \ln \ln(1 - F)^{-1} \) (= \( \ln(F) \) – \( \ln(e_t - e_{t,\text{min}}) \) relation is common for any \( F \) and therefore for any \( n \). Accordingly, the \( m \) value is determined also uniquely for any \( F \) and \( n \). Only the \( e_0 \) value is dependent on \( n \). In this way, though the actual number of strut was unknown, the obtained \( e_{t,\text{min}} \) and \( m \) values were reliable.

The following important indications could be read from the present statistical analysis.

1. Within the accuracy of the electric resistance measured in this work (Fig. 4(a) and (b)), the transition strain from stage II to III could not be identified. The transition strain could be estimated first by the statistical analysis which elucidated the value of \( e_{t,\text{min}} \) (= 1.7 and 0.86% for nickel and copper foams, respectively), corresponding to the transition strain from stage II to III.

2. Though the \( e_0 \) value was dependent on \( n \), it was commonly high for any \( n \) (0.24, 0.35 and 0.54 for \( n = 4648, 13944 \) and 46480, respectively). The average of \( e_t \) values, \( e_{\text{ave}} \), is given by \( e_{\text{ave}} = e_0 \Gamma(1 + 1/m) + e_{t,\text{min}} \). Taking the nickel foam as an example, \( e_{\text{ave}} \) is calculated to be 23, 33 and 50% for \( n = 4648, 13944 \) and 46480, respectively. In actual foam, \( n \) is larger at least than 4648. It is deduced that \( e_{\text{ave}} \) is, at least, higher than 23%. This result indicates that the geometry-affected failure strain of the struts in the foam is very high in comparison with the strain of around 5% (Fig. 4(b)) at ultimate stress of the foam. This means that the struts with lower \( e_t \) values (the struts with originally low failure strain and the struts whose longitudinal direction is not so much inclined to the tensile axis) are failed dominantly at low applied strains \( (e < 5\%) \). The preceding failures of struts act to raise the stress state of the neighboring struts and act as the seeds to cause failures of the struts successively beyond \( e \approx 5\% \). Such a situation takes place at the strain far lower than the average failure strain.

4. Conclusions

Tensile deformation and failure behavior of open cell nickel and copper foams at room temperature was studied experimentally and analytically. The main results are summarized as follows.

1. The deformation and failure progressed through the following four stages: stage I characterized by elastic deformation up to around 0.01% strain for both nickel and copper foams; stage II by plastic deformation without failure of struts (around 0.01%~1.7% (nickel foam), around 0.01%~0.86% (copper foam)); stage III by co-occurrence of plastic deformation and cumulative failure of struts (around 1.7%~5.2% (nickel foam), around 0.86%~6.2% (copper foam)); and stage IV by successive failure of struts nearly in a limited cross-section and large increase in electrical resistance with applied strain (5.2%~ (nickel foam), 6.2%~ (copper foam)).

2. The distribution of failure strain of struts in the cumulative failure region was described by the Weibull distribution, from which the strain at transition from stage II to III could be estimated. Also the result of the statistical analysis suggested that the average failure strain of the struts in the foam is much higher than the strain at ultimate stress of the foam.

REFERENCES